

analysis it is desirable to improve the accuracy of the measurements, and to extend them to (hkl) values and to other shrinkage stages. These experimental measurements are in progress.

We wish to acknowledge the help of Mr K. K. Møller who determined the absolute intensities of certain reflexions, and of Mr F. H. C. Crick and Mr H. E. Huxley who took some of the required photographs.

Note added in proof, 4 March 1952. It has now been found that $F(200)$ is positive, which excludes the

longer of the two alternative models and indicates $55 \times 55 \times 65 \text{ \AA}$ as the dimensions of the hydrated molecule.

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Short Communications

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Acta Cryst. (1952). **5**, 283

A note on the calculation of the absorption factors for single crystals with high absorbing power. By D. GRDENIĆ, *Chemical Institute, Faculty of Science, University of Zagreb, Zagreb, Yugoslavia*

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Recently Howells (1950) described a universal graphical method of estimating absorption factors for single crystals. This method is based on the application of the loci of points for which the optical path of X-rays is constant. The author (Grdenić, 1949) suggested a numerical method, based on the same principle, for calculating absorption factors for the zero-layer reflexions of a single crystal having the shape of a rectangular prism. This method, however, was intended for crystals of low or medium absorbing power. During the course of the structure analysis of mercury compounds (all having a high absorption coefficient) it was found that the absorption factors could be calculated more easily and rapidly by using simple formulae. It may be noted that the same is true of Howells's graphical method; it is very good when the absorption coefficient is not too high. For crystals with high absorbing power the use of formulae is much more practical. These formulae were obtained by a method similar to that of Hendershot (1937). Their application may best be explained using the same example as Howells (1950). All notations used here relate to Fig. 1 (p. 367) of his paper.

1. Reflexion 'on the crystal face'

In this case area (1) makes the main contribution to the reflected intensity, areas (2) and (4) make small contributions, while area (3) makes practically no contribution. The integral

$$A_{hkl} = \int_S \frac{\exp(-\mu x) ds}{S}$$

for area (1) gives the formula

$$A(1) = \frac{1}{S} \frac{1}{\mu (\operatorname{cosec} \psi_2 + \operatorname{cosec} \varphi_2)} \left[AB - \frac{\sin(\psi_2 + \varphi_2)}{\mu (\sin \psi_2 + \sin \varphi_2)} \right].$$

Substituting the values given by Howells for the reflexion 038 of mercury diphenyl we get $A(1) = 3.45 \times 10^{-2}$. If we evaluate the integral for areas (2) and (4) the formulae

$$A(2) = \frac{1}{S} \frac{\sin \varphi_1 \sin \varphi_2}{\mu^2 \sin \delta_1} \frac{1}{1 + \sin \psi_2 / \sin \varphi_2}$$

and

$$A(4) = \frac{1}{S} \frac{\sin \psi_1 \sin \psi_2}{\mu^2 \sin \delta_2} \frac{1}{1 + \sin \varphi_2 / \sin \psi_2}$$

are obtained, where δ_1 and δ_2 are the interfacial angles, in this case 104° and 76° respectively. Substituting the appropriate values, we get $A(2) = 0.11 \times 10^{-2}$ and $A(4) = 1.18 \times 10^{-2}$. Thus the total absorption factor is

$$A_{038} = A(1) + A(2) + A(3) + A(4) = 4.74 \times 10^{-2}.$$

The graphical method due to Howells gives $A_{038} = 4.69 \times 10^{-2}$, which proves that the agreement is satisfactory.

2. Reflexion 'on the corner'

In this case the incident rays fall on one face and the diffracted rays leave through the adjacent face. Only the region at the common crystal edge makes a contribution to the absorption factor. The above integral for this case gives the formula

$$A_{\delta} = \frac{1}{S} \frac{\sin \psi_1 \sin \psi_2}{\mu^2 \sin \delta},$$

ψ_1 and ψ_2 being now the angles made by the diffracted and incident rays, respectively, with the appropriate crystal faces (e.g. for the corner at B this formula is to be applied when the angle ψ_1 of the diffracted ray with BC is greater than 76° ; ψ_2 is then the angle of the incident ray with AB). In the case of mercury diphenyl, δ has

only the value δ_1 or δ_2 . It may be noted that the formula is no longer accurate when ψ_2 and φ_2 are nearly zero.

The above formulae are applicable to the zero-layer reflexions of any prism-shaped crystal of great absorbing power. They were applied successfully in the structure analysis (soon to be published) of mercury diethylene oxide ($\mu = 550 \text{ cm.}^{-1}$ for $\text{Cu } K\alpha$ radiation), the crystal of which had a hexagonal cross section perpendicular to the needle axis.

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Determination of interaxial angles of a triclinic crystal from a single setting. By G. B. CARPENTER, *Metcalf Research Laboratory, Brown University, Providence, Rhode Island, U.S.A.*

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Buerger (1942) has described how all parameters of the crystal lattice may be determined from a single setting of a triclinic crystal on a Weissenberg goniometer. This communication presents a simplified method for measuring the angles α and β (the axis of rotation is taken as c). Buerger suggests two methods for measuring these angles: the first (p. 377) depends on measuring the height above the film center line of the bottom of the festoon $h01$ for α (and $0k1$ for β); the second (p. 383)

of Weissenberg photograph shown on the right. The ($h01$) spots which appear on the photograph enable the $h01$ and $\bar{h}01$ festoons to be drawn in, as well as their common asymptote. The vertical distance $2Y'_\alpha$ between the festoons is then measured at the intersection of the asymptote with the center line. Then the angle Y_α (rad.) is equal to Y'_α/r , where r is the camera radius. For a camera of 57.3 mm. diameter, $Y_\alpha(^{\circ}) = 2Y'_\alpha$ (mm.). The angle α is then calculated from these relations, which follow from Fig. 1 and from Buerger's treatment:

$$\delta_\alpha = R_\mu(1 - \cos Y_\alpha),$$

where $R_\mu = (\cos \mu)/\lambda$ is the radius of the circle of reflection in the layer with equi-inclination angle μ ;

$$\tan \alpha = -\zeta/\delta_\alpha;$$

$$\zeta = 1/c.$$

Geometrical consideration of the effect of various errors yields the following results. A 1° error in mis-setting the equi-inclination angle μ or in aligning the c axis with the axis of rotation causes no more than a $\frac{1}{2}^\circ$ error in the value of α , provided $c/\lambda \leq 10$. Since the shortest axis is usually chosen to rotate the crystal about, this requirement is usually satisfied. A 2° error in locating the point of intersection of the asymptote with the center line (corresponding to 1 mm. along the center line on the 57.3 mm. diameter camera) causes no more than a $\frac{1}{2}^\circ$ error in the value of α , provided $c/\lambda \leq 10$. A 1° error in Y_α (corresponding to a 1 mm. error in the measurement of $2Y'_\alpha$ with the 57.3 mm. diameter camera) causes no more than a 2.5° error in α , provided $c/\lambda \leq 10$.

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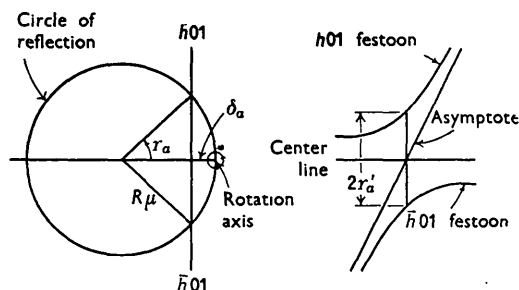


Fig. 1. Left: The intersection of the sphere of reflection with the first layer of the reciprocal lattice. Right: The corresponding section of a Weissenberg photograph.

requires a specially prepared photograph, the necessity for which is often not evident until the first layer has been recorded. The procedure described below is more accurate than the first and, unlike the second, is applied to the normal record of the first layer.

As in Buerger's procedure, we require the perpendicular displacement δ_α of the reciprocal lattice row $h01$ from the intersection of the rotation axis with the first layer (and similarly for β). The left diagram in Fig. 1 illustrates the orientation of the first layer of the reciprocal lattice at the instant it is recorded in the center of the portion